

## Session Types

- Session types specify communication **protocols** and statically guarantee that concurrent programs respect them.

```

S ::= !A.S           send value of type A then continue as S
| ?A.S             receive value of type A then continue as S
| ⊕{Li : Si} select label Li then continue as Si
| &{Li : Si} offer branches Li with continuations Si
| End

```

## Session-Typed Communication

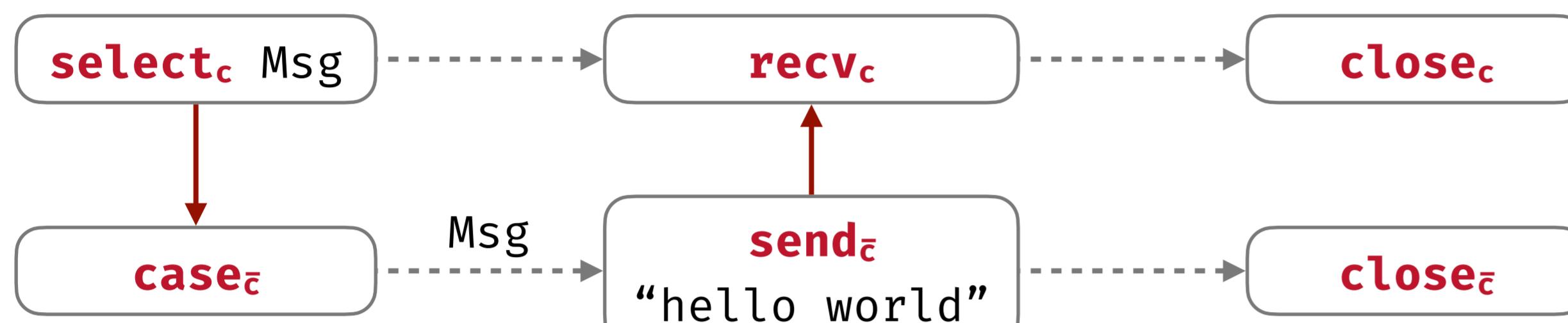
- Concurrent programs communicate via **dual channels**:

```

c : ⊕{Msg : ?String.End}
c̄ : &{Msg : !String.End}

fork [c : ⊕{Msg : ?String.End}]
  (selectc Msg; val x = recvc; print x; closec)
  (casec̄ { Msg ↦ sendc̄ "hello world"; closec̄ })
  hello world

```



# Session-Typed Effect Handlers

Wen-hao Tang  
The University of Edinburgh



## Protocols for Effects and Handlers

- Inspired by session types, we use **protocols** specified by **behavioural effect types** to describe the interaction between effects and handlers.
- A naive protocol for one unidirectional effect and deep handler:

```

c : ⊕{Ask : () ⇒ Int}
  invoke Ask (any times) on the channel c
c̄ : &{Ask : () ⇒ Int}
  (deeply) handle Ask on the dual channel c̄

```

- A protocol for two effects:

```

c : ⊕{Choose : () ⇒ Bool; Ask : () ⇒ Int}
  invoke Choose and Ask
c̄ : &{Choose : () ⇒ Bool; Ask : () ⇒ Int}
  handle Choose and Ask

```

## Handling Effects on the Dual Channel

- Inspired by the channels, effects must and can only be handled in the **dual** channel. Different channels never interfere with each other.

```

fork [c : ⊕{Ask : () ⇒ Int}]
  (doc Ask + doc Ask)
  (handlec̄ oc̄ { case Ask r ↦ r 21 })

  doc Ask --> doc Ask
  doc Ask --> handlec̄
  handlec̄ --Ask--> pure comp

```

- Channels generalise *handler names* since multiple handlers can share one channel:

```

fork [c : ⊕{Choose : () ⇒ Bool; Ask : () ⇒ Int}]
  (if (doc Choose) then 7 else doc Ask)
  (handlec̄ (handlec̄ oc̄ { case Choose r ↦ r true + r false }))
  { case Ask r ↦ r 35 }

```

```

doc Choose --> doc Ask
doc Ask --> handlec̄
handlec̄ --Choose--> pure comp
pure comp --Ask--> handlec̄
handlec̄ --Ask--> pure comp

```

## Algebraic Effects and Handlers

- Algebraic effects and handlers allow programmers to define, customise, and compose a range of crucial programming features modularly.

```

handle (do Ask + do Ask) { case Ask r ↦ r 21 }
  21 + handle (do Ask) { case Ask r ↦ r 21 }
  21 + 21
  42

```

```

handle (handle (if (do Choose) then 7 else do Ask)
  { case Choose r ↦ r true + r false })
  { case Ask r ↦ r 35 }
  handle ( if true then 7 else do Ask
    + if false then 7 else do Ask)
  { case Ask r ↦ r 35 }
  handle (7 + do Ask) { case Ask r ↦ r 35 }
  42

```

## Effect Types

- For soundness, the type system is usually extended with an **effect system** to track the effects used by programs.

```

f : () {Ask : () ⇒ Int} → Int
f _ = do Ask + do Ask

```

```

g : () {Choose : () ⇒ Bool; Ask : () ⇒ Int} → Int
g _ = if (do Choose) then 7 else do Ask

```

## Bidirectional Interaction of Effects and Handlers

- Behavioural effect types can easily encode **bidirectional effects**.
- 2-layer bidirectional interaction:

```

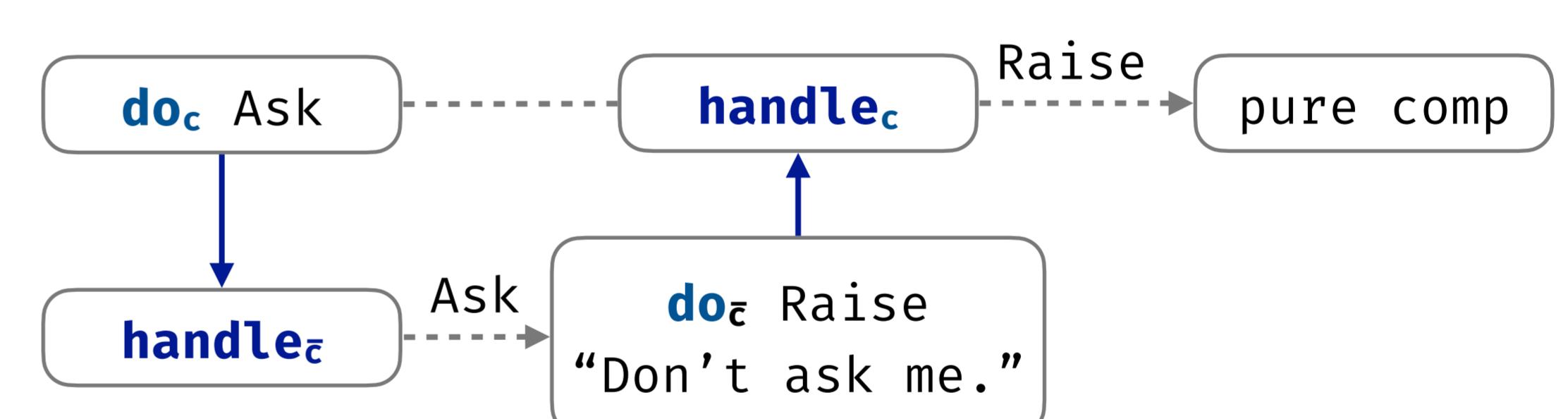
c : E = ⊕{Ask : () → Int : &{Raise : String → ⊥}}
  invoke Ask, then must handle Raise outside
c̄ : E = &{Ask : () → Int : ⊕{Raise : String → ⊥}}
  handle Ask, then can invoke Raise when resuming

```

```

fork [c : E]
  (handlec (40 + doc Ask) { case Raise s r ↦ print ("Error: " ++ s)})
  (handlec̄ oc̄ { case Ask r ↦ r {doc̄ Raise "Don't ask me."} })

```

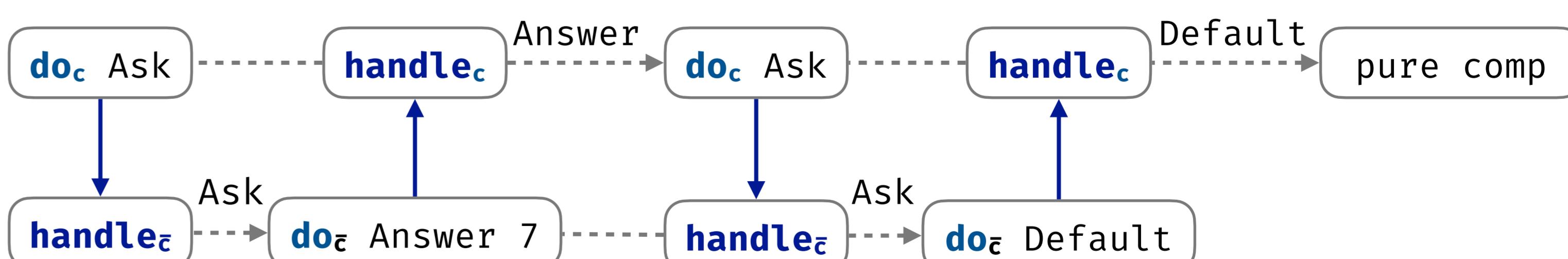


- 4-layer bidirectional interaction:

```

c : E = ⊕{Ask: &{Answer: ⊕{Ask: &{Default}}}}
fork [c : E]
  (handlec (doc Ask) { case Answer x r ↦ r {
    handle (x + doc Ask)
    { case Default r ↦ r 35 }
  } })
  (handlec̄ oc̄ { case Ask r ↦ r {
    handle (doc̄ Answer 7)
    { case Ask r ↦ r {doc̄ Default}}
  } })

```



## Future Work

- Pretty much work in progress.
- Some interesting or necessary things we are working on:
  - first-class or second-class **linear channels** with **shallow handlers**
  - truly concurrency semantics
  - "standard" metatheory, polymorphism, subtyping, recursive types, etc